Conservation Contracts for Exhaustible Resources

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Conservation Contracts

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- Only in 2000-2012, tropical rainforest in South America was reduced by 4.2%, in Asia by 12.5%, and in Africa by 2.8%.
- Deforestation in the tropics has contributed to 30% of man-made CO₂ emissions, and it contributes to 10-20% of annual greenhouse gas emissions.
- Negative externalities \$2-4.5 trillion a year (the Economist, 2010)
- Deforestation could be halved at a cost of \$21-35 billion per year.

- **Contracts Exists:** The United Nations, the World Bank, and the Norwegian government are offering financial incentives to countries successful in reducing deforestation.
- Contracts are signed with an increasing number of countries: Brazil, Indonesia, Guyana, Ethiopia, Vietnam, Mexico, Tanzania, Congo.
- **Simple contracts**: Rates are harmonized and constant: 5 USD/ton avoided CO2, for every unit of deforestation less than some (negotiated) benchmark
- Limited success so far / Too early to judge

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 - We may have to compensate the owners/users....
 - ...but who/how/when/where?
- We don't know.
- First (?) paper on how to contract on slowing resource depletion. (well...not yet a paper...but in progress)

Literature (preliminary)

• Hotelling '31: Optimal depletion of exhaustible resource

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 - Today: dynamic model of contracting in the presence of externalities

- A Model of Extraction
- The First Best
- The Equilibrium
- Generalizations
- Policies
- Conclusions

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• Common discount factor $\delta \in [0, 1]$

• Timing: In each period, the principal offers contracts, then agents extract.

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- Reasonable if:

$$y_i^t < \widetilde{y} \equiv (1-\delta) b/2a.$$

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Proposition

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- The first best
- Sequence: Given x^t, x^t_i is irrelevant
 Steady state: y^T ≡ ∑_i y^T_i = 0 if b > e, y^T = y⁰ if b < e.

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- Sequence: Extract all stocks at the same time
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- The first best
- **Sequence:** Given x^t , x_i^t is irrelevant
- **2** Steady state: $y^T \equiv \sum_i y_i^T = 0$ if b > e, $y^T = y^0$ if b < e.
- Speed: Marginal social revenue increases exponentially

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- In steady state, $\sum_i s_i^t = \sum_i y_i^t (b ay_i^t)$ is concave. Thus, it is more expensive to compensate a *large* number of wannabe monopolists, than to compensate one big

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- Can order according to size, $y_1^0 \ge y_2^0 \ge ... \ge y_n^0$.

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- A unique steady state is reached in finite time T.
- If b > e, $y^T = 0$, as in the first best
- If b < e, the i largest stocks are conserved where i satisfies

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Proposition

- A unique steady state is reached in finite time T.
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With a large number of small stocks (y_j → 0), the steady-state conservation level is

$$y^T = \max\left\{0, \frac{e-b}{a}\right\}.$$

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Figure: The largest stocks are conserved, while the smallest stocks are depleted.

Proposition

• For any two consecutive periods, we have:

$$\left[b - e - a(2 - w)x^{t}\right] + a\sum_{i=1}^{i-1} y_{i}^{0} = \delta\left[b - e - a(2 - w)x^{t+1}\right]$$

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- The marginal social surplus increases more than exponentially in time.
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- The outcome is first best if n = 1
- Otherwise, the speed of extraction is too high.

• Suppose marginal extraction costs are c_i and environmental harm e_i .

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Sequence: j should be extracted from first if c_j + e_j < c_i + e_i, but will be, in equilibrium, iff:

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Steady state: Nothing (more) should be extracted from i if c_i + e_j > b, but nothing will be, in equilibrium, iff:

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The equilibrium speed is given by:

$$b - e_i - c_i - a(2 - w) x^t + a \sum_{\substack{i=1 \\ \text{Visc}}}^{i-1} y_i^t = \delta \left[b - e_i - c_i - a(2 - w) x^{t+1} \right]$$
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Extensions

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Country\Year	Forest Cover	Deforestation	Illegal logging
	2000 (1000 ha)	2000-2010	in 2013
Brazil	545943	5%	> 50%
Cameroon	22116	10%	65%
Ghana	6094	19%	70%
Indonesia	99409	5%	60%
Laos	16433	6%	80%
Malaysia	21591	5%	35%
Papua New Guinea	30133	5%	70%
Rep. Congo	22556	1%	70%

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Enforcement Expenditures



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- If y_i^t x_i^t is conserved, the profit from illegal logging is p^t at each unit of the forest.
- Expected penalty must be at least as large as the profit
- The cost of monitoring is thus $\alpha p^t (y_i^t x_i^t)$ for some $\alpha \ge 0$. So,

$$u_i^t = \beta p^t x_i^t - \alpha p^t \left(y_i^t - x_i^t \right) - c_i x_i^t + s_i^t,$$

- This is the model of Harstad and Mideksa (ReStud, '17)
- (That paper also studies contracting with a subset of agents, and endogenizes institutions/(de)centralization. But the model is static..)
- All results above continue to hold, qualitatively.

- Above we have assumed that the outside option is $x_i^t = y_i^t$
- Unreasonable unless each period long/ δ is small
- In steady state, each i is a potential monopolist and would like to extract f_i (y^t_i) if ignoring the contract.
- Suppose outside option is indeed some increasing $f(y_i^t) \in [0, y_i^t]$.
- Results above tend to hold, qualitatively.

Proposition

• The smallest is extracted first iff $\alpha < \alpha_1$

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- **(**) The extraction speed is too fast iff $\alpha < \alpha_3$
 - For larger *α*, the results are overturned.

Robustness: The Crucial Assumptions

Extract from *i* first iff:

$$(c_j + e_j) - (c_i + e_i) > \frac{a}{1 - \delta} \begin{bmatrix} \beta \left[H(y_i) - H(y_j) \right] \\ -(\alpha + \beta) \left[H(F(y_i)) - H(F(y_j)) \right] \end{bmatrix},$$

where $H(y_i) = z - \delta F_i(z)$. The r.h.s. is positive if $y_i > y_j$ iff

$$\frac{\alpha}{\beta} < \alpha_1 = \frac{H(y_i) - H(y_j)}{H(F(y_i)) - H(F(y_j))} - 1.$$

Too much is extracted from i iff:

$$\frac{\alpha}{\beta} < \alpha_{2} = \frac{\sum_{j \neq i} y_{j} - F(y_{j})}{\sum_{j \neq i} F(y_{j})} = \frac{\sum_{j \neq i} y_{j}}{\sum_{j \neq i} F(y_{j})} - 1 > 0$$

The speed is too large iff:

$$\frac{\alpha}{\beta} < \alpha_{3} = \frac{1}{(1-\delta)} \left[\frac{\sum_{j \neq i} y_{j}^{t}}{\sum_{j \neq i} F_{j} \left(y_{j}^{t} \right)} - 1 \right]$$

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Current Research: Dynamics



• If strong/coal: conserves everything in the largest district

• If weak/forests/illegal: conserves everything in the smallest district

- It might indeed be efficient to offer contracts to the largest tropical forest owners, such as Brazil and Indonesia, according to this theory
- However, the optimal contracts are highly asymmetric
- Harmonized contracts achieve too little conservation at a too large cost.

Policies and Comparative Static

• With *m* similar buyers with demand function $p^t = b - a_m x_m^t$, aggregate demand is $p^t = b - ax^t$ where $1/a = \sum_m 1/a_m$

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 - Steady state conservation decreases
 - Speed of extraction increases

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With commitment, payments can be delayed This relaxes incentive constraints in the meanwhile ...and then, there is no reason to raise x_i^t to lower s_j^t Outcome becomes first-best (after the very first period) If principal can ask for money up front, first-best also in first period. Long-term contracts lead to slower extraction and more conservation.

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 - Boycotts makes the equilibrium worse.

Robustness: Non-negative side payments

- Going back in time, x^t increases and p^t decreases
- This reduces the temptation to "extract it all" and waiting becomes more attractive
- It is possible that $s_i^t = 0$ is sufficient
- When $s_j^t = 0$, there is less need to raise x_i^t , since s_j^t cannot be reduced further.
- If s_j^t = 0 for many agents, conservation will take place in any case, and the principal may be better off waiting before entering the game
- This is the opposite of the "Green Paradox"
- Equilibrium may be in mixed strategies (Harstad '16).

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